

Regimes of Wetting Transitions on Superhydrophobic Textures Conditioned by Energy of Receding Contact Lines

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We discuss an evaporation-induced wetting transition on superhydrophobic stripes, and show that depending on the elastic energy of the deformed contact line, which determines the value of an instantaneous apparent contact angle, two different scenarios occur. For relatively dilute stripes the receding angle is above 90° , and the sudden impalement transition happens due to an increase of a curvature of an evaporating drop. For dense stripes the slow impregnation transition commences when the apparent angle reaches 90° and represents the impregnation of the grooves from the triple contact line towards the drop center.

Introduction. — On a superhydrophobic (SH) surface, which is both rough and hydrophobic, the contact angle of water is very large,¹ and two states are possible for a drop. In the Wenzel state water penetrates the texture completely,² but in the Cassie state air is trapped by texture, so that liquid sits on the top of the asperities.³ In most applications (microfluidics, “self-cleaning”, water-repellent materials, bio-medical devices) the Cassie state is desired, which, however, could be unstable or metastable, so that irreversible transitions towards the more stable Wenzel state can be provoked.^{4–7}

During the last decade, much insight has been gained into the relative stability of the Cassie state, the Cassie-to-Wenzel wetting transition. Several criteria to determine a preferable state have been suggested.^{1,8} If the liquid/air interfaces are flat (very large drops), then for a texture with a given roughness r (ratio between the actual surface area of a rough solid and its projected surface area) and solid-liquid fraction, ϕ_S , Cassie and Wenzel angles are equal for a material with Young’s angle θ_c defined as⁹

$$\cos \theta_c = \frac{\phi_S - 1}{r - \phi_S}. \quad (1)$$

The Cassie state should be stable if $\theta > \theta_c$, while the Wenzel state is preferred at $\theta < \theta_c$. Hence, no stable Cassie state is possible on hydrophilic textures. These relation, however, becomes invalid for small drops due to a Laplace pressure, $\Delta p = 2\gamma/R$, where γ is the surface tension and R is the drop radius. Accounting for this pressure difference gives a more general thermodynamic criterion for the stability of the Cassie state:⁸ $(\gamma + h\Delta p) \cos \theta_c - \gamma \cos \theta > 0$, where h is the depth of the texture. For low ϕ_S these criteria deny the observed experimentally Cassie state suggesting it is metastable. To interpret these several models have been proposed,^{7,10,11}

such as a touching the bottom side of the texture⁷ or reaching the local advancing contact angle on a vertical side of the texture.^{12,13}

Most investigations of a wetting transition have been conducted with a dilute array of SH pillars due to their remarkable wetting properties. In this letter we study the wetting transition on textures decorated by highly anisotropic SH grooves and vary ϕ_S in a very large range. Such textures, which do not necessarily provide large apparent contact angles, now become extremely important in the context of microfluidic applications.¹⁴ For instance, dilute SH stripes show the remarkable drag-reducing ability.^{15,16} Dense SH grooves generate transverse hydrodynamic phenomena¹⁷ and can be successfully used to separate tiny particles^{18,19} or enhance mixing rate^{20,21} in microfluidic devices. These striped textures amplify electrokinetic pumping^{22,23} and are employed for sorting droplets.^{24–26}

We study a wetting transition by monitoring the evaporation of a drop. An evaporating drop is known to produce various intriguing phenomena, such as coffee stains²⁷ or wine tears,²⁸ and has been already studied with isotropic SH surfaces,^{7,29,30} although the quantitative understanding is still at its infancy. During the evaporation the drop becomes smaller and the contact angle retracts. At some moment the transition to the Wenzel state occurs.

Some recent results may add a new dimension to the problem of evaporation-induced wetting transition. It has been shown^{31,32} that for relatively low ϕ_S , the receding (i.e. the smallest possible) angle, $\cos \theta_r^*$, on the SH surface, which is above 90° , depends significantly on the elastic energy of the deformed contact line. During receding the contact line is bent at the gas areas being pinned at solid areas. The value of a receding angle on a striped SH surface can then be evaluated as:³¹

$$\cos \theta_r^* = -1 + \phi_S(1 + \cos \theta_r) - \frac{2a + 1}{2} \phi_S^2 \ln \phi_S, \quad (2)$$

where θ_r is the receding angle of the material. The non-linear (logarithmic) term here includes the parameter a ,

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which reflects the relative length of a side part of the pinned contour. This term represents an elastic contribution to $\cos \theta_r^*$, which has been found to be large even at moderate ϕ_S . It is therefore natural to assume that an elastic distortion of the contact line could be important in determining the onset of the evaporation-induced wetting transition. All existing approaches neglect the contribution of the triple contact line to the energy of the system (except some qualitative free energy arguments^{33,34}) and we are unaware of any prior work that has addressed this issue.

The aim of our letter is to explore experimentally and to discuss quantitatively the possible effect of the contact line elasticity on the wetting transitions. We show here that it is generally neither small nor negligible, and that depending on the degree of elastic deformation of the contact line two physically different scenarios, fast impalement and slow imbibition, could occur.

Experimental. – SH rectangular grooves (see Fig. 1) of width w separated by distance d (both varied from 3 to 25 μm) and depth h (5 μm) have been prepared to provide $\phi_S = d/(w + d)$ from 0.12 to 0.88 in the Cassie state. SH surfaces were made of polydimethylsiloxane by replication of silicon masters (Fig. 1(b,c)). The masters fabricated by projection lithography have been purchased from AMO GmbH, Germany. They have been oxidized by plasma treatment in evacuated chamber with oxygen flow 30 mL/min and plasma power 200 W (PVA TePla 100 Plasma System), and coated with a trichloro(1H,1H,2H,2H-perfluorooctyl)silane (PFOTCS, 97%, Sigma Aldrich) through the gas phase in evacuated dessicator at pressure 80 mbar for 3 hours. After removal of a bowl with PFOTCS from dessicator it was evacuated to full vacuum for 15 minutes in order to remove formed clusters of PFOTCS from the silicon surface. Hydrophobized surfaces have been rinsed by isopropanol. Afterwards we fabricated hydrophobic PDMS replicas from silicon patterns by a common soft lithography³⁵ (Sylgard®184 Silicone elastomer KIT, Dow Corning). Flat surface of such PDMS showed a receding angle $\theta_r = 84^\circ$ and advancing angle $\theta_a = 115^\circ$.

SEM images were taken using a Hitachi S-4800 field emission scanning electron microscope. Texture geometry has been characterized by interference profilometry (WYKO NT2000, Veeco, USA) and optical microscopy (Axioplan 2 Imaging System, Zeiss, Germany).

To study CWT we monitored evaporation of milli-Q water droplet deposited onto a surface^{7,29} at room temperature and ambient atmospheric pressure. Measurement of evolution of droplet geometrical parameters, namely radius R , contact angle θ^* and base diameter D (see Fig. 1), were performed with use of Drop Shape Analysis System DSA100 (Krüss, Germany). Current SH wetting state of the drop was monitored by optical microscopy (Axioplan 2 Imaging System, Zeiss, Germany) equipped with a CCD camera recording up to 25 frames per second. The typical initial volume of the droplet for all types of measurements was 2 μL .

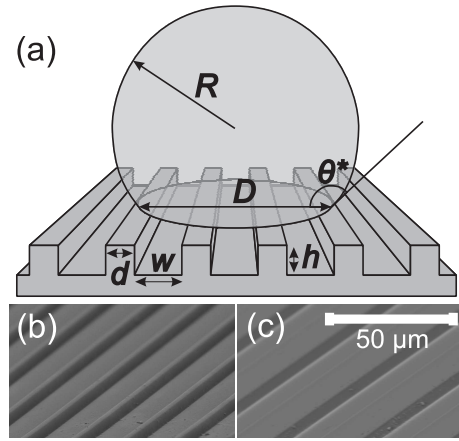


FIG. 1. Sketch of droplet settled on the SH stripes (a) and microphotographs of superhydrophobic surfaces with $\phi_S = 0.49$ (b) and 0.33 (c) fabricated by a soft lithography

Results and discussion. – During the evaporation the decrease of a droplet volume (and the increase of its curvature) is generally accompanied by a retraction of a triple contact line. Fig. 2 illustrates the typical changes of the instantaneous apparent contact angle and the base diameter during the evaporation. All measurements suggested that θ^* is practically isotropic despite the anisotropy of the texture. We recall that observations of an isotropic receding angle for a drop on striped surfaces have been reported before.^{31,36} Note however that the transverse angle shows irregular oscillations of a period $w + d$, more pronounced for textures with larger w .

For relatively dilute patterns (see Fig. 2(a)) an evaporation represents a three-stage process. On the first stage we observe a decrease in θ^* at a nearly constant (due to a pinning of a contact line on defects) base diameter, D . During the second stage the contact angle reaches its minimum value, θ_r^* (above 90°), and remains constant as the drop evaporates. The contact line becomes completely unpinned and slides fast. However, this state changes when the drop becomes smaller than a critical radius, R^* . Then, the angle suddenly decreases, which implies a sharp increase in D . The contact line is very efficiently pinned, and the angle gradually vanishes, from an initial value down to zero, despite the hydrophobicity of the material. This behavior results from an impalement of the drop in the texture.⁷ Note that the impalement time is well below 40 ms. We remark that these observations are qualitatively similar to made before for dilute pillars.^{12,33}

For dense patterns the evaporation occurs in two stages (see Fig. 2(b)), and the first one is identical to observed for dilute patterns. The evolution of a contact angle is smooth and does not indicate the difference between two steps of evaporation. However, the dependence of D on time represents a piecewise function with a distinct fold point, which corresponds to $\theta^* \simeq 90^\circ$, where the second

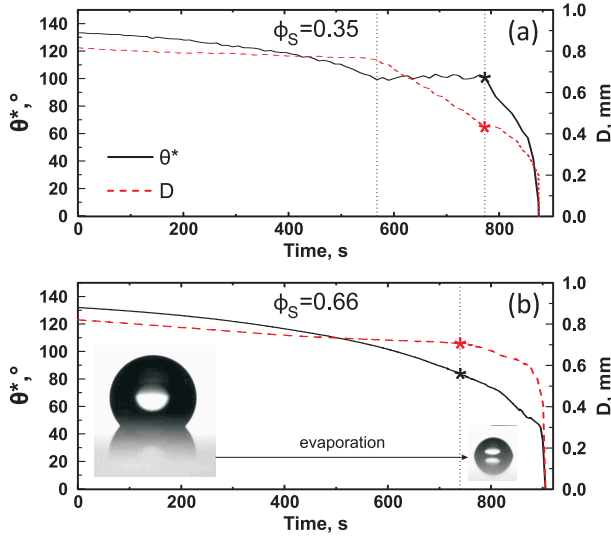


FIG. 2. Typical dependence of an apparent contact angle (solid curve) and a drop base diameter D (dashed curve) on time during evaporation for $\phi_S = 0.35$ (a) and $\phi_S = 0.66$ (b). The symbols mark the transition points.

stage commences. Then, the base diameter starts to decrease much faster, and the contact angle vanishes. This behavior can be interpreted as resulting from a wetting transition, which is much slower than for dilute patterns and obviously involves a completely different scenario we discuss below.

Fig. 3 shows values of θ^* of a wetting transition as a function of ϕ_S observed experimentally. Also included are the theoretical calculations with Eq.(2) with the value $a = 3.1 \pm 1.3$ obtained from fitting. Note that this value is close to previously obtained by a different method.³¹ A general conclusion from this plot is that there are two distinct regimes of the wetting transition depending on ϕ_S . In the first regime the elastic deformation of the contact line on the strong defects (see inset in Fig. 3) reaches its maximum providing the receding angle above 90° . In the second regime the maximum deformation and a corresponding receding angle cannot be attained since when θ^* reaches the value of 90° the Cassie state becomes thermodynamically unstable. By using Eq.(2) we can now define a value of a solid fraction, ϕ_S^* , which determines a criterion of two regimes of a wetting transition for a striped surface

$$1 = \phi_S^*(1 + \cos \theta_r) - \frac{2a+1}{2}(\phi_S^*)^2 \ln \phi_S^*, \quad (3)$$

which for our surfaces gives $\phi_S^* \simeq 0.4$.

In the first regime, $\phi_S < \phi_S^*$, where a wetting transition commences at θ_r^* defined by Eq.(2), the Cassie state is generally metastable according to Eq.(1), so that the curvature of the evaporating drop is expected to provoke a transition. We have therefore measured the critical radius of the evaporating droplet, R^* , which leads to a transition, and the results are shown in Fig. 4. Let us now

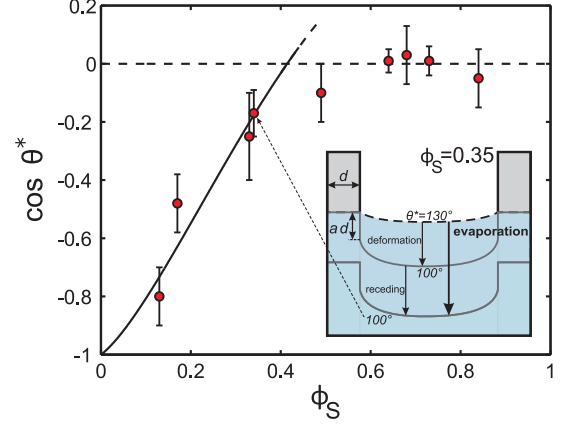


FIG. 3. Effective contact angle of the wetting transition as a function of ϕ_S . Red circles show experimental data, solid curve plots theoretical predictions (Eq. 2), dashed line corresponds to 90° . Inset shows (top view) sketch of a deformed contact line on the stripes with $\phi_S = 0.35$

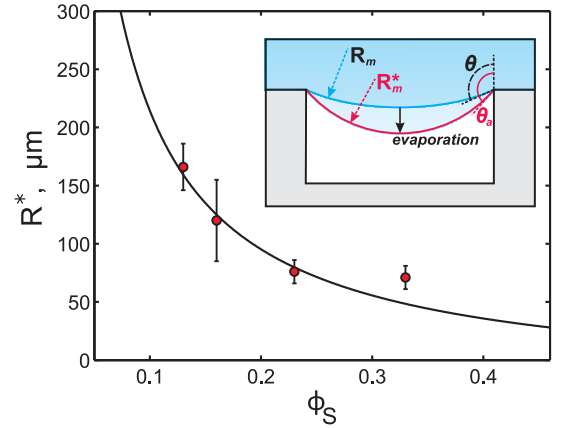


FIG. 4. The critical radius of the drop provoking a transition as a function of ϕ_S for the surfaces with $d = 5\mu\text{m}$. Circles show experimental data, the solid curve is the prediction of Eq.(4). Inset shows an evolution of a meniscus during evaporation.

examine why a transition should take place. We first note that for our textures we have to rule out a mechanism related to touching the bottom part of texture by meniscus,⁷ which would be typical for very dilute patterns. According to a criterion, $|\cos \theta_a| = 4hw/(4h^2 + w^2)$,¹² such a scenario could be expected only for a texture with a twice larger w than we use here, i.e. our textures are not dilute enough to expect such a scenario. Therefore, our transition is likely provoked by a violation of the pressure balance due to a bending of a meniscus between neighboring stripes.^{12,13} This balance can be written as $\Delta p(1 - \phi_S) = \gamma\Lambda |\cos \theta|$,^{12,37} where Δp is a Laplace pressure, Λ is a density of contact line (i.e. a length of the triple contact line per unit area), and the instantaneous

local contact angle θ is on the edge of the groove (relative to a vertical (side) wall as seen in Fig. 4). The Laplace pressure under meniscus is $\Delta p = 2\gamma/R = \gamma/R_m$, where R_m is the radius of cylindrical meniscus, and the contact line density is $\Lambda = 2/(w+d) = 2\phi_S/d$. Therefore, for stripes $(1-\phi_S)/R = |\cos\theta|/(w+d)$. During the evaporation both the meniscus curvature and the instantaneous local contact angle (relative to a side wall), θ , increase. The transition then occurs when the local contact angle reaches its maximum attainable value $\theta = \theta_a$. Thus the critical drop radius is

$$R^* = \frac{d(1-\phi_S)}{\phi_S |\cos\theta_a|}. \quad (4)$$

Note that it depends not only on ϕ_S , but also on the spacing between stripes d and properties of a material. The predictions of Eq.(4) are included in Fig. 4 and are in excellent agreement with experimental data. Thus, Eq.(4) taken together with Eq.(2) defines a criterion for a wetting transition on a relatively dilute stripes. We note that the strategy of our analysis for a striped SH surface is similar to previously suggested for isotropic array of pillars,¹² although the relevance to $\cos\theta_r^*$, which depends on the contact line elasticity, remained obscure before.

In the second regime, $\phi_S > \phi_S^*$, the stage of a constant θ_r^* is not reached owing to the thermodynamic limitations. The surface becomes no longer effectively hydrophobic on the first stage of the evaporation. In this situation the values of R^* were found to vary significantly between different measurements and also depend on the initial drop volume. These suggest that the transition is not really controlled by the curvature of the drop. The optical observations show that when θ^* reaches 90° , the liquid starts to impregnate the grooves (see Fig. 5). We remark and stress that the onset of the transition is local. It starts at the triple contact line, but closer to center of the droplet the Cassie state is kept. Similar observations have been mentioned before.^{5,38,39} Our work thus allows one interpreting them in terms of the elastic energy of the deformed contact line. Note that our impregnation velocity is $10\text{--}20\text{ }\mu\text{m/s}$, so that the impregnation transition time is of the order of 10 s, i.e. several orders of magnitude exceeds the impalement transition time in case of dilute patterns.

Conclusion. – We have studied the wetting transition on striped Cassie surfaces with a different fraction of solid areas. Our experiment demonstrated that that depending on the fraction of the solid area, and, therefore, elastic energy of the deformed contact line, two qualitatively different scenarios of the transition occur. For relatively dilute stripes we have observed the sudden impalement transition controlled by a curvature of an evaporating drop. For dense stripes the slow impregnation transition commences when the Cassie surface becomes effectively hydrophilic due to a decrease in an apparent receding angle. This transition represents the impregnation of the grooves from the triple contact line towards the drop cen-

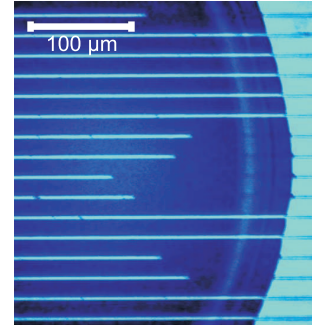


FIG. 5. Experimental recording of the imbibition of the grooves during a wetting transition on the texture with $\phi_S = 0.86$.

ter. We provide theoretical arguments, which allowed us to quantify and control both types of the wetting transition. Our interpretation thus allows one to use different recipes for avoiding this detrimental effect in experimental studies and various applications.

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